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## ఎిజయ : గృణిత

## Subject : MATHEMATICS

( ఇంగ్లిజ్ భాజాంతర / English Version )
( ๔ళి జఠ్యృస్రు / Old Syllabus )


దినాంも : 21. 09. 2020 ]
[ Date: 21.09. 2020


[ Max. Marks : 100

## General Instructions to the Candidate :

1. This Question Paper consists of 50 objective and subjective types of questions.
2. This question paper has been sealed by reverse jacket. You have to cut on the right side to open the paper at the time of commencement of the examination. Check whether all the pages of the question paper are intact.
3. Follow the instructions given against both the objective and subjective types of questions.
4. Figures in the right hand margin indicate maximum marks for the questions.
5. The maximum time to answer the paper is given at the top of the question paper. It includes 15 minutes for reading the question paper.
I. Four alternatives are given for each of the following questions / incomplete statements. Only one of them is correct or most appropriate. Choose the correct alternative and write the complete answer along with its letter of alphabet.

$$
8 \times 1=8
$$

1. If $A=\{a, b, c, d, e\}$ and $B=\{a, m, n, d\}$ then $A \cap B$ is
(A) $\{a, d, e\}$
(B) $\{m, n\}$
(C) $\{a, d\}$
(D) $\{a, b, c, d, e, m, n\}$
2. If two lines are mutually perpendicular, then the product of their slopes is
(A) -1
(B) 0
(C) $\frac{1}{2}$
(D) 1 .
3. The sum of first 20 natural numbers is
(A) 142
(B) 210
(C) 254
(D) 310 .
4. If ${ }^{n} P_{2}=90$, then the value of $n$ is
(A) 8
(B) 9
(C) 10
(D) 12 .
5. A cubical die whose faces numbered from 1 to 6 is rolled once. The probability of getting a perfect square number on its top face is
(A) $\frac{1}{6}$
(B) $\frac{2}{6}$
(C) $\frac{3}{6}$
(D) 1 .

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6. If the mean of 5 scores is 6 , then the sum of all the scores is
(A) 11
(B) 26
(C) 30
(D) 42 .
7. If $p(x)=3 x^{2}-2 x+5$, then the value of $p(-1)$ is
(A) 4
(B) 6
(C) 8
(D) 10 .
8. The distance of the point $P(3,4)$ from $y$-axis is
(A) 3 units
(B) 4 units
(C) 5 units
(D) 7 units.
II. Answer the following questions :
9. Write the H.C.F. of any two prime numbers.
10. Write the degree of the polynomial $g(x)=4 x^{5}-6 x^{3}+2 x^{2}+5$.
11. Define concentric circles.
12. If $\cos x=\frac{24}{25}$, then what is the value of $\sec x$ ?
13. In $\triangle A B C$, if $A B^{2}+B C^{2}=A C^{2}$, then name the right angle.
14. The area of the base of a right circular cone is $100 \mathrm{~cm}^{2}$ and height is 3 cm . Find its volume.
III. Answer the following questions :
15. Classify the following situations as examples of Permutations and Combinations:
i) Arranging 6 different books on a shelf
ii) Selecting 2 black balls from a bag containing 3 red and 4 black balls
iii) Forming a committee of 4 members from a group of 12 persons
iv) Forming 3 -digit numbers using 1, 4, 5 and 7 .
16. Find the sixth term of the Geometric Progression $2,6,18, \ldots$ by using a suitable formula.

OR
Find the sum of the Geometric series $1+\frac{1}{2}+\frac{1}{4}+\ldots$ up to $\infty$.
17. If $8, x-1,16$ are in Arithmetic Progression, then find the value of $x$.
18. Prove that $(2+\sqrt{3})$ is an irrational number.
19. Three fair coins are tossed together. Find the probability of getting utmost one head.
20. Find the product of $\sqrt{2}$ and $\sqrt[3]{3}$.
21. Rationalise the denominator and simplify :

$$
\frac{\sqrt{6}+\sqrt{5}}{\sqrt{6}-\sqrt{5}}
$$

22. Find the remainder obtained when $p(x)=3 x^{2}-5 x+6$ is divided by $g(x)=(x-2)$ using Remainder theorem.

OR

Find the quotient and remainder using synthetic division.

$$
\left(2 x^{3}+3 x^{2}-x+6\right) \div(x-2)
$$

23. In the given figure in $\triangle A B C, X Y \| B C$. If $B X=7 \mathrm{~cm}, A X=5 \mathrm{~cm}$ and $A C=18 \mathrm{~cm}$, then find $C Y$.


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24. Prove that: $\left(1-\cos ^{2} \theta\right)\left(1+\cot ^{2} \theta\right)+\tan ^{2} \theta=\sec ^{2} \theta$.
25. Find the distance of the point $P(5,12)$ from the origin.
26. In a class of 60 students, everyone should select to study either Mathematics or Science or both subjects. If $75 \%$ of students select Mathematics, $50 \%$ of students select Science, then find how many students select both the subjects.
27. The maximum number of diagonals that can be drawn in a polygon is 9 . Find the number of sides.
28. The length of a rectangular field is three times its breadth. If the area of the field is $192 \mathrm{~m}^{2}$, then find its breadth.
29. Draw a circle of radius 3 cm . Construct a pair of tangents to it such that the angle between them is $60^{\circ}$.
30. Draw a plan for the plane ground using the information given below :
( Scale $20 \mathrm{~m}=1 \mathrm{~cm}$ )

|  | To C ( in metre ) |  |
| :---: | :---: | :---: |
|  | 200 |  |
| To D 120 | 140 |  |
|  | 100 | 60 to B |
| To E 80 | 60 |  |
|  | From A |  |

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31. In the given figure $O$ is the centre of the circle. Name
i) the biggest chord
ii) a secant.

32. In how many ways can 6 different books be arranged on a shelf ?
33. The mid-point of the line segment joining the points $A(-2,4)$ and $B(6, m)$ is $C(2,1)$. Find the value of $m$.
34. $A$ and $B$ are two non-disjoint subsets of a Universal set. Represent
$(A \cup B)^{\prime}$ by a Venn diagram.
35. The following table shows the number of students of a class how they come to school. Draw a pie-chart to represent this.

| Walk | Bicycle | Bus | School van |
| :---: | :---: | :---: | :---: |
| 14 | 10 | 3 | 9 |

36. Find the value of $p$ for which the quadratic equation $x^{2}-p x+16=0$ has equal roots.
37. In the given figure in $\triangle A B C, \angle B A C=90^{\circ}, A D \perp B C$. If $B D=4 \mathrm{~cm}$, $D C=5 \mathrm{~cm}$, then find the value of $x$.

38. If $\cos 4 A=\sin 5 A$, where $4 A$ and $5 A$ are acute angles, then find the value of $A$.
39. Find the equation of a line whose angle of inclination is $45^{\circ}$ and $y$-intercept is 3 .
40. The total surface area of a solid hemisphere is $1848 \mathrm{~cm}^{2}$. Find its radius. [ Use $\pi=\frac{22}{7}$ ]
IV. Answer the following questions :
41. In a Harmonic Progression, the third term is $\frac{1}{7}$ and fifth term is $\frac{1}{11}$. Find its tenth term.

The fourth term of an Arithmetic Progression is 6 more than its second term. If the eighth term is 26 , then find the Arithmetic Progression.

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42. The total runs scored by two cricket players $A$ and $B$ in 15 matches are 1050 and 900 with standard deviations 5.6 and 3.0 respectively.
i) Who is better run getter ?
ii) Find who is more consistent in performance.
43. If one root of the equation $x^{2}+p x+q=0$ is 3 times the other, then prove that $3 p^{2}=16 q$.

## OR

Solve by using formula: $(2 m+3)(3 m-2)+2=0$.
44. Prove that "if two circles touch each other externally, then the centres and the point of contact are collinear".
45. In an equilateral triangle $A B C, A N \perp B C$. Prove that $A N^{2}=3 B N^{2}$.

In $\triangle A B C, A B=A C$ and $D$ is any point on $B C$ as shown in the figure. Prove that $A B^{2}-A D^{2}=B D . D C$.


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46. The angle of elevation of the top of a vertical pole from a point on a horizontal ground is $30^{\circ}$. On walking 5 m towards the pole the angle of elevation is found to be $45^{\circ}$. Find the height of the pole.

## OR

Prove that $\frac{\sin \theta}{1+\cos \theta}+\frac{1+\cos \theta}{\sin \theta}=2 \operatorname{cosec} \theta$.
V. Answer the following questions :
47. Prove that "the areas of two similar triangles are proportional to the squares on the corresponding sides". 4
48. A cylindrical vessel of base diameter 28 cm is filled with some quantity of water. A metallic solid sphere of radius 7 cm is completely immersed in the vessel so that no water expells from the vessel. Find the height of water level raised in the vessel. [ Use $\pi=\frac{22}{7}$ ]


OR
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The volume of a frustum of a cone shaped dustbin is $26,994 \mathrm{~cm}^{3}$. If the radii of the two circular ends are 15 cm and 8 cm , then find the height of the dustbin. [ Use $\pi=\frac{22}{7}$ ]
49. Solve graphically : $x^{2}-x-6=0$.
50. Construct a direct common tangent to two circles of radii 4 cm and 2 cm whose centres are 9 cm apart. 4

